Essential Physics I

英語で物理学の エッセンス|

Lecture 4: 9-05-16

This lecture



Understand why circular motion does not have constant acceleration



Be able to calculate the orbit of a satellite



Know Newton's 3 force laws



Contradict conspiracy theories about the moon landing





Calculate the motion of a flying pig

Review

Motion under gravity



Motion can be split into components

Constant acceleration equations can be used on each component.

$$v_{0,x} = v\cos\theta$$

$$v_x = v_{x,0} + a_x t$$

$$x = x_0 + v_{x,0} t + \frac{1}{2} a_x t^2$$

$$v_x^2 = v_{x,0}^2 + 2a_x (x - x_0)$$

$$v_{0,y} = v\sin\theta$$

$$v_{y} = v_{y,0} + a_{y}t$$

$$y = y_{0} + v_{y,0}t + \frac{1}{2}a_{y}t^{2}$$

$$v_{y}^{2} = v_{y,0}^{2} + 2a_{y}(y - y_{0})$$

uniform motion

Is circular motion the same as projectile motion?



uniform motion



 $\rightarrow \overline{v}$ velocity vector $\rightarrow \overline{a}$ acceleration vector



Is circular motion the same as projectile motion?



In both cases, acceleration magnitude is constant.

But in circular motion, the vector direction changes.

Therefore, no! Circular motion is different from projectile motion.

Circular motion acceleration is called the centripetal acceleration.

uniform motion





uniform motion



uniform motion

Velocity components:



$$v = \sqrt{v_x^2 + v_y^2}$$

Position components:



$$r = \sqrt{x^2 + y^2}$$



 $|\bar{r}_1| = |\bar{r}_2| = r$ $|\bar{v}_1| = |\bar{v}_2| = v$

 $\bar{r}_1 \neq \bar{r}_2$ $\bar{v}_1 \neq \bar{v}_2$

magnitude equal

direction different

From diagram:



and since \overline{v} is perpendicular (90° angle) to \overline{r} :



 Δv γ ${\mathcal U}$

uniform motion



If θ is small, $\Delta r \simeq s$, curve distance between P_1 and P_2 .

 $s = \text{distance travelled in time, } \Delta t$ = $v \Delta t$

Therefore:



$$a = \frac{v^2}{r}$$

uniform circular motion

Example



A satellite at altitude 300 km has a period T = 1.5h. What is its centripetal acceleration?

 $r = R_E + \text{altitude}$ $= (6.37 \times 10^6 \text{m}) + (300 \text{km}) \times \frac{1 \times 10^3 \text{m}}{1 \text{km}}$ $= 6.67 \times 10^6 \text{m}$



one orbit
$$= 2\pi r = 2\pi (6.67 \times 10^6) \text{m}$$

 $T = 1.5\text{h} = 1.5\text{h} \times \frac{3600\text{s}}{1\text{h}} \text{s}$
 $V = \frac{2\pi r}{T} = 7,757 \text{m/s}$

 $a = \frac{v^2}{r} = \frac{4\pi^2 r}{T^2} = 9.0 \,\mathrm{m/s^2}$

Why not $9.81 \mathrm{m/s^2}$?

Example

Quiz

A tethered ball moves in a horizontal circle of radius 2 m. It makes one revolution in 3 s.

Find its acceleration.







A tethered ball moves in a horizontal circle of radius 2 m. It makes one revolution in 3 s.

Find its acceleration.

 8.76m/s^2 direction outwards (a) (b) 8.76m/s^2 direction inwards 8.76m/s^2 direction same as velocity **(C)** (d) 62.3m/s^2 direction outwards $62.3 m/s^2$ (e) direction inwards 62.3m/s^2 direction same as velocity (f)



A tethered ball moves in a horizontal circle of radius 2 m. It makes one revolution in 3 s.

Find its acceleration.

r

$$v = \frac{2\pi r}{T} = \frac{2\pi (2 \text{ m})}{3 \text{ s}} = 4.19 \text{ m/s}$$
$$a = \frac{v^2}{T} = \frac{(4.19 \text{ m/s})^2}{(4.19 \text{ m/s})^2} = 8.76 \text{ m/s}^2$$

 $2\,\mathrm{m}$







What are forces?



Forces change motion:



Forces are vectors:



Rules for forces

Newton's First Law

"A body in uniform motion remains in uniform motion, and a body at rest remains at rest, unless acted on by a nonzero net force."



If you don't change it, it won't change

Quiz

Newton's First Law

But a rolling ball comes to a stop. Why?

(A) there always has to be a continual force to keep moving

(B) there is a force acting that stops the ball

(C) because "rolling" is a different kind of motion

(D) Newton's laws don't always apply

Newton's First Law

If the Earth disappeared, what path would the moon follow?

(A) continue on red path

(B) move on green path

(C) move on blue path

(D) stop



Newton's First Law

Circular motion is not uniform.

 $ar{r}, ar{v}, ar{a}$ vectors change direction continuously.

Therefore, circular motion requires a net force .

The moon would move with the velocity it had at the point the Earth vanished.



Rules for forces

Newton's First Law

- If Newton's first law applies, we are in an inertial reference frame.
- Rotating frames are not inertial.
- A car moving at a constant velocity is an inertial frame.



- Newton's laws will hold inside and outside the car.
- Experiments done inside and outside the car will give the same result.

(B)

Quiz

Newton's First Law

Apollo 11 landed on the moon in 1969.

Some people have claimed the moon landing was fake.

One reason they give is that the American flag waves, yet there is no wind on the moon.

Why is this reason invalid?



(A) There is wind on the moon.

The flag moves as the astronauts set it down, and doesn't stop.

(C) Oh my God! There was no moon landing!



Rules for forces



Newton's 2nd Law

"The rate at which a body's momentum changes is equal to the net force acting on the body."

Quantifies) the effect of force on motion.

calculate exactly

The effect of a force depends on an object's mass and velocity The product of mass and velocity is momentum $\bar{p} = m\bar{v}$ multiply $\bar{F}_{net} = \frac{d\bar{p}}{dt} = \frac{(m\bar{v})}{dt} = m\frac{d\bar{v}}{dt} = m\bar{a}$





Nobody likes change.... The resistance to movement is called inertia.

The more difficult it is to change the motion of an object the more inertia it has.

$$\bar{a} = \frac{\bar{F}_{net}}{m}$$
 Forces have a smaller
effect if the mass is big
mass measures inertia small inertia

Quiz

Newton's 2nd Law

A force produces an acceleration of 150 m/s^2



The same force gives a 2nd can an acceleration of 50 m/s². What is the mass of the second can?

Quiz



The same force gives a 2nd can an acceleration of 50 m/s². What is the mass of the second can?

(a) 0.005 kg (b) 0.015 kg (c) 0.045 kg (d) 22.2 kg

Quiz



The same force gives a 2nd can an acceleration of 50 m/s². What is the mass of the second can?

$$\bar{F} = m_1 \bar{a}_1 = m_2 \bar{a}_2$$

0.015 kg × 150 m/s² = m₂ × 50 m/s²
$$m_2 = \frac{0.015 \text{ kg} \times 150 \text{ m/s}^2}{50 \text{ m/s}^2}$$

Example

Newton's 2nd Law

A particle of mass 0.4 kg is subjected to 2 forces, $\bar{F}_1 = 2N\bar{i} - 4N\bar{j}$ and $\bar{F}_2 = -2.6N\bar{i} + 5N\bar{j}$.



Particle starts from rest (v = 0) at the origin (x = 0) at t = 0, find its position and velocity at t = 1.6s

Example

Newton's 2nd Law

How to solve:



motion from a constant force

Use $\bar{F}_{net} = m\bar{a}$:

constant force



constant acceleration

constant acceleration equations



 $v = v_o + at$ $x = x_o + v_o t + \frac{1}{2}at^2$ $v^2 = v_o^2 + 2a(x - x_o)$

Example

Newton's 2nd Law



A particle of mass 0.4 kg is subjected to 2 forces, $\bar{F}_1 = 2N\bar{i} - 4N\bar{j}$ and $\bar{F}_2 = -2.6N\bar{i} + 5N\bar{j}$.

Particle starts from rest (v = 0) at the origin (x = 0) at t = 0, find its position and velocity at t = 1.6s

Net force: $\overline{F}_{net} = \overline{F}_1 + \overline{F}_2 = (2N\overline{i} - 4N\overline{j}) + (-2.6N\overline{i} + 5N\overline{j})$ = $-0.6N\overline{i} + 1.0N\overline{j}$

From Newton's 2nd: $\bar{a} = \frac{\bar{F}_{net}}{m} = \frac{-0.6N\bar{i} + 1.0N\bar{j}}{0.4kg}$ or $a_x = -1.5m/s^2$ and $a_y = 2.5m/s^2$

Example

Newton's 2nd Law

$$a_x = -1.5 {
m m/s}^2$$
 , $a_y = 2.5 {
m m/s}^2$

Horizontal:

$$x = x_0 + v_{x,0}t + \frac{1}{2}a_xt^2 = \frac{1}{2}(-1.5\text{m/s}^2)(1.6\text{s})^2 = -1.92\text{m}$$

$$v_x = v_{x,0} + a_xt = (-1.5\text{m/s}^2)(1.6\text{s}) = -2.40\text{m/s}$$

$$0'$$

Vertical:

$$y = v_0 + v_{y,0}t + \frac{1}{2}a_yt^2 = \frac{1}{2}(2.5\text{m/s}^2)(1.6\text{s})^2 = 3.20\text{m}$$
$$v_y = v_{y,0} + a_yt = (2.5\text{m/s}^2)(1.6\text{s}) = 4.00\text{m/s}$$



Newton's 2nd Law



Position: $-1.92\overline{i} + 3.20\overline{j}$ m

Velocity: $\overline{v} = -2.40\overline{i} + 4.00\overline{j}$ m/s

Rules for forces



"If object A exerts a force on object B, then object B exerts an oppositely directed force of equal magnitude on A"

Forces come in pairs:

If I push you with a force F, then I feel a force F on me





If you kick a bowling ball, it hurts!

Newton's 3rd Law

Strange but true (and sad...!)

You weigh more than you think

 $F_{\rm scale}$

Gravity pulls you down

But when you stand on the scales, they exert an upwards force on you.

$$ar{F}_{
m net} = ar{F}_g + ar{F}_{
m scale}$$
 weight

"the normal force", \bar{n}







Quiz

 $F_{
m scale}$

How different is your weight?



$$\bar{F}_{\rm net} = \bar{F}_g + \bar{F}_{\rm scale}$$

Newton's 2nd law: $\bar{F}_{net} = m\bar{a}$ Circular motion: $a = \frac{v^2}{r}$ Gravitational force: $\bar{F}_g = -mg$ $g = 9.81 \text{m/s}^2$ Earth's radius: $R_E = 6.37 \times 10^6 \text{m}$ I orbit = I day

Is the answer closest to: (a) 10 % (b) 1 % (c) 0.1 % (d) 0.01 %

Quiz



 $\bar{F}_g = ?$ How different is your weight? $\bar{F}_{
m scale}$



$$\frac{F_g}{\bar{F}_{\text{scale}}} = \frac{mg}{mg - mr\left(\frac{2\pi}{24 \times 3600\,\text{s}}\right)^2} =$$

= 0.0034 = 0.34%

The flying pig (conical pendulum)



0

What is the time for one orbit?

The flying pig (conical pendulum)



0

What is the time for one orbit?

What do we know?



0

Motion is horizontal, so no net vertical acceleration: $a_{y,net} = 0$

But there is centripetal acceleration: $a_{x,net} = \overline{a}_c$



Let's look at Newton's 2nd law....



Since force is a vector, we can look at each component



 F_{q}

mq



From:

$$=2\pi\sqrt{\frac{D\sin}{a_{\rm x,net}}}$$

•

θ

$$a_{\mathrm{x,net}} = g \tan \theta$$

$$T = 2\pi \sqrt{\frac{D\cos\theta}{g}}$$

$$=2\pi\sqrt{\frac{0.97\mathrm{m}\cos 37^\circ}{9.81\mathrm{m/s}^2}}=1.8\mathrm{s}$$

Problem solving

- (I) Draw a diagram
- (2) Balance the forces
- (3) Consider each component

(4) Get full marks

 $F_{\rm x,net} = ma_x$ $v_x = v_{x,0} + a_x t$ $x = x_0 + v_{x,0}t + \frac{1}{2}a_xt^2$ $v_x^2 = v_{x,0}^2 + 2a_x(x - x_0)$ $F_{\rm y,net} = ma_y$ $v_{y} = v_{y,0} + a_{y}t$ $y = y_{0} + v_{y,0}t + \frac{1}{2}a_{y}t^{2}$ $v_y^2 = v_{y,0}^2 + 2a_y(y - y_0)$ $a = \frac{v^2}{r}$

Problem solving

- A 2 kg picture is hung by 2 wires of equal length. Each makes an angle $\theta = 30^{\circ}$ with the horizontal.
- Find the tension in the wires.





Problem solving

A 2 kg picture is hung by 2 wires of equal length. Each makes an angle $\theta = 30^{\circ}$ with the horizontal.

Find the tension in the wires.

vertical
$$\bar{F} = m\bar{a}$$

 $F_g = T\sin\theta + T\sin\theta = mg$
 $T = \frac{mg}{2\sin 30^\circ} = \frac{2 \text{ kg} \times 9.81 \text{ m/s}^2}{2 \sin 30^\circ}$



 $= 19.62 \,\mathrm{N}$

A bucket of water is whirled in a vertical circle of radius, γ .





quiz

A bucket of water is whirled in a vertical circle of radius, γ .

- If its speed is v_t at the top of the circle, find the force (as an expression)exerted on the water, \bar{F}_p , by the bucket at the top of the circle.
- If r = 1m, what is the minimum v_t for which the water will remain in the bucket?

$$\bar{F}_p = ?$$

$$\bar{v}_{t,\min} = ?$$



A bucket of water is whirled in a vertical circle of radius, \mathcal{T} .

- If its speed is v_t at the top of the circle, find the force (as an expression)exerted on the water, \bar{F}_p , by the bucket at the top of the circle.
- If r = 1m, what is the minimum v_t for which the water will remain in the bucket?
- (a) $\bar{v}_{t,\min} = 6.21 \text{m/s}$
- (b) $\bar{v}_{t,\min} = 5.4 \text{m/s}$
- (c) $\bar{v}_{t,\min} = 1.24 \text{m/s}$

(d) $\bar{v}_{t,\min} = 3.13 \mathrm{m/s}$





Since F_p cannot exert upwards force on the bucket, minimum OK speed at top is when $F_p = 0$.

 $mg = m \frac{v_{t,\min}^2}{r}$ $v_{t,\min} = \sqrt{rg} = \sqrt{1 \,\mathrm{m} \times 9.81 \,\mathrm{m}} = 3.13 \,\mathrm{m/s}$



quiz



Physics in the World



Skydiver Felix Baumgartner on track for super jump



By Jonathan Amos Science correspondent

Motion in ID

Constant acceleration





What to look for



WHAT was discovered?

HOW was it done?

WHY is it exciting?



WHAT

Skydive from 71,500 ft

Austrian skydiver Felix Baumgartner is well on the way to setting a world record for the highest free-fall jump.

On Thursday, the adventurer leapt from a balloon-borne capsule 71,500ft (22km) above New Mexico, landing safely eight minutes later.

The dive was intended to test all his equipment before he tries to free-fall from 120,000ft later this year.

In doing so, he would better the mark of 102,800ft set by US Air Force Colonel Joe Kittinger in 1960.

Even just Thursday's jump puts Baumgartner in a select group as only Kittinger and Russian Eugene Andreev have descended from higher.

Baumgartner, who is famous for stunts such as jumping off the Petronas Towers, is seen in the special pressure suit he must wear to stay alive in the thin air and extreme cold of the stratosphere.

WHY

Practice for world record skydive

Already #3 in the world

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his **Red Bull Stratos** team estimates he reached 364mph (586km/h) during the descent, and was in free fall for three minutes and 43 seconds before opening his parachute. From capsule to ground, the entire jump lasted eight minutes and eight seconds.

8 minute 8 second jump with top speed, 364 mph.

The 42-year-old was quoted afterwards as saying that the cold was hard to handle.

"I could hardly move my hands. We're going to have to do some work on that aspect," he said.

The Austrian also said the extraordinary dimensions of the high atmosphere took some getting used to: "I wanted to open the parachute after descending for a while but I noticed that I was still at an altitude of 50,000ft."

Not easy!

Cold may still be a problem on the big jump



Summary

Skydiver Felix Baumgartner jumped from 71,500 ft.

This was a practice for a world record attempt.

This jump was the 3rd highest ever attempted.



The jump lasted 8 minute 8 seconds with a top speed of 364 mph. HOW

His **Red Bull Stratos** team estimates he reached 364mph (586km/h) during the descent, and was in free fall for three minutes and 43 seconds before opening his parachute. From capsule to ground, the entire jump lasted eight minutes and eight seconds.

Estimate the acceleration

(a)
$$a = 170 \text{ m/s}^2$$

(b) $a = 9.81 \text{ m/s}^2$
(c) $a = 2.63 \text{ m/s}^2$
(d) $a = 0.73 \text{ m/s}^2$



quiz

His **Red Bull Stratos** team estimates he reached 364mph (586km/h) during the descent, and was in free fall for three minutes and 43 seconds before opening his parachute. From capsule to ground, the entire jump lasted eight minutes and eight seconds.

Estimate the acceleration

 Δv

$$a_{\text{average}} = \overline{\Delta t}$$

$$\Delta v = 586 \,\frac{\text{km}}{\text{h}} = \left(586 \,\frac{\text{km}}{\text{h}}\right) \left(\frac{1000 \,\text{m}}{1 \,\text{km}}\right) \left(\frac{1 \,\text{h}}{3600 \,\text{s}}\right) = 163 \,\text{m/s}$$

$$\Delta t = 3 \,\text{min} + 43 \,\text{s} = (3 \,\text{min}) \left(\frac{60 \,\text{s}}{1 \,\text{min}}\right) + 43 \,\text{s} = 223 \,\text{s}$$

$$a = \frac{163 \,\text{m/s}}{223 \,\text{s}} = 0.73 \,\text{m/s}^2$$



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Why is
$$a
eq 9.81 \, \mathrm{m/s^2}$$
 ?

(a) There is a mistake in this article

(b) A second force is acting

(c) Gravity is not constant so high up

(d) Equations do not apply in real life





When a massive star ($\sim 1.4-3~\times M_{\rm sun}$) dies, it can leave a neutron star.

Neutron stars are massive but tiny!

Gravitational acceleration is therefore HUGE $g_{\rm neutron} \sim 10^{12} \,{
m m/s}^2$



If Felix jumped from 22 km above the surface of a neutron star, how long until he hit the star?

(a) I day(b) I minute(c) I second(d) I millisecond(e) 0.1 millisecond(f) 0.01 millisecond

quiz

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$$y = y_0 + v_{y,0}t + \frac{1}{2}a_yt^2$$

$$0 = 22,000 + 0t + \frac{1}{2}(-10^{12})t^2$$

 $t = 0.2 \,\mathrm{ms}$

This lecture



Understand why circular motion does not have constant acceleration



Be able to calculate the orbit of a satellite



Know Newton's 3 force laws



Contradict conspiracy theories about the moon landing





Calculate the motion of a flying pig